



Standard Practice for Dealing With Outlying Observations¹

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Note—Corrections were made to Table 2 and the year date was changed on Sept. 7, 2016.

1. Scope

1.1 This practice covers outlying observations in samples and how to test the statistical significance of outliers.

1.2 The system of units for this standard is not specified. Dimensional quantities in the standard are presented only as illustrations of calculation methods. The examples are not binding on products or test methods treated.

1.3 *This standard does not purport to address all of the safety concerns, if any, associated with its use. It is the responsibility of the user of this standard to establish appropriate safety and health practices and determine the applicability of regulatory requirements prior to use.*

2. Referenced Documents

2.1 *ASTM Standards:*²

E456 Terminology Relating to Quality and Statistics

E2586 Practice for Calculating and Using Basic Statistics

3. Terminology

3.1 *Definitions*—The terminology defined in Terminology E456 applies to this standard unless modified herein.

3.1.1 *order statistic* $x_{(k)}$, n —value of the k th observed value in a sample after sorting by order of magnitude. **E2586**

3.1.1.1 *Discussion*—In this practice, x_k is used to denote order statistics in place of $x_{(k)}$ to simplify the notation.

3.1.2 *outlier*—see **outlying observation**.

3.1.3 *outlying observation*, n —an extreme observation in either direction that appears to deviate markedly in value from other members of the sample in which it appears.

¹ This practice is under the jurisdiction of ASTM Committee E11 on Quality and Statistics and is the direct responsibility of Subcommittee E11.10 on Sampling / Statistics.

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² For referenced ASTM standards, visit the ASTM website, www.astm.org, or contact ASTM Customer Service at service@astm.org. For *Annual Book of ASTM Standards* volume information, refer to the standard's Document Summary page on the ASTM website.

4. Significance and Use

4.1 An outlying observation, or “outlier,” is an extreme one in either direction that appears to deviate markedly from other members of the sample in which it occurs.

4.2 Statistical rules test the null hypothesis of no outliers against the alternative of one or more actual outliers. The procedures covered were developed primarily to apply to the simplest kind of experimental data, that is, replicate measurements of some property of a given material or observations in a supposedly random sample.

4.3 A statistical test may be used to support a judgment that a physical reason does actually exist for an outlier, or the statistical criterion may be used routinely as a basis to initiate action to find a physical cause.

5. Procedure

5.1 In dealing with an outlier, the following alternatives should be considered:

5.1.1 An outlying observation might be the result of gross deviation from prescribed experimental procedure or an error in calculating or recording the numerical value. When the experimenter is clearly aware that a deviation from prescribed experimental procedure has taken place, the resultant observation should be discarded, whether or not it agrees with the rest of the data and without recourse to statistical tests for outliers. If a reliable correction procedure is available, the observation may sometimes be corrected and retained.

5.1.2 An outlying observation might be merely an extreme manifestation of the random variability inherent in the data. If this is true, the value should be retained and processed in the same manner as the other observations in the sample. Transformation of data or using methods of data analysis designed for a non-normal distribution might be appropriate.

5.1.3 Test units that give outlying observations might be of special interest. If this is true, once identified they should be segregated for more detailed study.

5.2 In many cases, evidence for deviation from prescribed procedure will consist primarily of the discordant value itself. In such cases it is advisable to adopt a cautious attitude. Use of one of the criteria discussed below will sometimes permit a clearcut decision to be made.